Lateral Variations in Upper Mantle Shear Wave Attenuation

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We study the lateral variations in shear wave at-tenuation in the upper mantle by analyzing the spec-tra from S and SS arrivals from selected seismograms in the IRIS FARM database between 1988 and 1999 in the IRIS FARM database between 1988 and 1999. We use seismograms from shallow earthquakes (≤ 50 km depth) at epicentral distances of 40^o-80^o for S waves and 80^o-160^o for SS waves. Each spectrum is the product of source, receiver, and propagation response functions as well as local source- and receiver-side ef-fects. We correct each spectrum for the known in-strument response, a source model with an ω^{-2} falloff at high frequencies, and a one-dimensional Q_{β} model. Since there are multiple receivers for each source and Since there are multiple receivers for each source and multiple sources for each receiver, we can approximate the source- and receiver-side terms by stacking the ap-propriate S log spectra. The resulting source-specific response functions include any remaining source spec-trum and the effect of near-source attenuation in the upper mantle; the receiver stacks include the site re-sponse and near-receiver Q structure. We correct the SS log spectra for the appropriate source- and receiver-side stacks found from the S waves. Since attenuation So tog spectra to the appropriate source random interview side stacks found from the S waves. Since attenuation in the lower mantle is small, the residual SS log spectrum approximates attenuation in the upper mantle near the SS bounce point, and can be used to estimate near the SS bounce point, and can be used to estimate δt^* at frequencies between 0.01 and 0.1 Hz. The result-ing bounce point δt^* measurements, which we smooth into caps of 5° radius, show spatially coherent patterns of more and less attenuating regions. We will compare these patterns with our previous results using the same method for higher-frequency P wave attenuation and with other studies of lateral variations in shear wave attenuation.

S32C MC: Hall D Wednesday 1330h

Wave Propagation Theory and Modeling Posters (joint with NG)

Presiding: B Milkereit, Dept. of Physics, University of Toronto

S32C-0638 1330h POSTER

Modal Decomposition of the Scattered Teleseismic Wavefield

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versity of British Columbia, 147-2219 Main Mall, Vancouver, BC V6T 1Z4, Canada The teleseismic P-coda contains energy scattered through a range of different mechanisms which include forward P-to-S scattering and back scattering created through free-surface reflection of the primary P-phase. Our focus in this study is the approximate separation of these different scattering modes in 1-D media using an inverse scattering formalism. It is well known that the forward problem of predicting wave scattering from het-erogeneity can be described through the Born series, an iterated form of the Lippman-Schwinger equation. In-dividual terms in this series represent the contributions of different orders of scattering interaction to the scat-tered wavefield. The inverse-scattering series, by anal-ogy, represents the heterogeneity in terms of different orders of the wavefield. The first term in the inverse series is derived through the Born approximation, and constitutes a distorted image of material property per-turbations which possesses many attributes/artifacts of the data. By operating on this image with the appro-priate component of the reference Green's function, it is possible to separate forward P-to-S conversions and free-surface P and S multiples. However, wavefield sep-aration is complicated by i) contrasting sensitivities of different scattered modes to heterogeneity, and ii) in-stabilities incurred through finite frequency bandwidth. These complications may be alleviated to some degree These complications may be alleviated to some degree through different forms of model regularization. We demonstrate this approach on synthetic seismograms and data collected from the Yellowknife Seismic Array, and consider the implications for multichannel wave-form inversion.

S32C-0639 1330h POSTER

Improved Mesh Interpolation for Ray Tracing by Wavefront Construction Methods for Anisotropic Media

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Ray methods are useful for the calculation of Green's tensors for three-dimensional, anisotropic me-dia because they are much faster than more exact al-gorithms such as finite differences. At the same time, there are significant challenges because of difficulties in implementation, particularly those related to the solu-tion of the two-point problem. Classical shooting meth-ods often either fail to determine a solution and can be very slow. Some approaches, such as eikonal meth-ods, are fast, but they do not compute amplitudes, con-sider only first arrivals, and cannot be easily applied to anisotropic models. Therefore, they cannot be used to compute Green's tensors. Wavefront construction methods, on the other hand, Ray methods are useful for the calculation of

Wavefront construction methods, on the other hand. do evaluate both traveltime and amplitude throughout an earth model (e.g., Lambaré et al., 1996). By track-ing propagating wavefronts, the geometry of an entire field of rays can be taken into account, and Green's ten-sors can be computed for the entire model space. These algorithms begin with a small number of rays traced di-rectly from the source. At regular increments in trav-eltime, a mesh is constructed from the set of points on all rays at the time of interest. As the wavefront prop-agates away from the source, new rays are inserted into the mesh based on an interpolation criterion. Previous implementations for isotropic media have typically in-serted new rays either when the separation between ex-isting rays exceeds an arbitrary distance or when wave-front curvature exceeds some threshold value. Because most rays are computed for only a portion of the overall time of propagation, the simulation requires less time do evaluate both traveltime and amplitude throughout time of propagation, the simulation requires less time overall

In our current implementation for anisotropic me-dia, we pose the wavefront construction method as a process of adaptive mesh construction, and we seek to increase the speed of the algorithm in several ways that distinguish it from other approaches. First, rather than applying dynamic ray tracing, we perform only kine-matic ray tracing, relying on finite-difference methods to compute derivatives of traveltime and other quan-tities with respect to ray coordinates. This provides a much simpler algorithm, especially for anisotropic media, and we suggest that because the equations are simpler, it can be faster. Secondly, we have developed a new interpolation criterion that tests the true error in traveltime across the mesh. Specifically, we test a new interpolation criterion that tests the true error in traveltime across the mesh. Specifically, we test calculations of traveltime at an existing mesh point by extrapolating from nearby rays using the paraxial method. Because the correct traveltime at the test point is accurately known from ray tracing, we can cal-culate the mismatch between this true value and the paraxial approximation. If the error exceeds a thresh-old level, we interpolate the mesh, ensuring that parax-ial methods allow us to compute traveltimes and am-improvement over previous algorithms because the er-ror is easily related to numerical error in the traveltime computation, unlike, for example, the distance thresh-old approach which requires an *ad hoc* definition of a maximum distance of accuracy. We will illustrate the implementation of the new interpolation scheme and show examples of applications to anisotropic media.

S32C-0640 1330h POSTER

Validation of Born Traveltime Kernels

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Princeton, NJ 08544, United States Most inversions for Earth structure using seis-mic traveltimes rely on linear ray theory to trans-late observed traveltime anomalies into seismic velocity anomalies distributed throughout the mantle. However, ray theory is not an appropriate tool to use when ve-locity anomalies have scale lengths less than the width of the Freesnel zone. In the presence of these struc-tures, we need to turn to a scattering theory in order to adequately describe all of the features observed in the waveform. By coupling the Born approximation to ray theory, the first order dependence of heterogene-ity on the cross-correlated traveltimes (described by the Fréchet derivative or, more colourfully, the banana-doughnut kernel) may be determined. To determine for what range of parameters these banana-doughnut kernels outperform linear ray theory, we generate several random media specified by their sta-tistical properties, namely the RMS slowness perturba-tion and the scale length of the heterogeneity. Acoustic

waves are numerically generated from a point source using a 3-D pseudo-spectral wave propagation code. These waves are then recorded at a variety of prop-agation distances from the source introducing a third parameter to the problem: the number of wavelengths traversed by the wave. When all of the heterogeneity has scale lengths larger than the width of the Fresnel zone, ray theory does as good a job at predicting the cross-correlated traveltime as the *banan-doughnut* ker-nels do. Below this limit, wavefront healing becomes a significant effect and ray theory ceases to be effec-tive even though the kernels remain relatively accurate provided the heterogeneity is weak.

tive even though the kernels remain relatively accurate provided the heterogeneity is weak. The study of wave propagation in random media is of a more general interest and we will also show our measurements of the velocity shift and the variance of traveltime compare to various theoretical predictions in a circum program. a given regime

S32C-0641 1330h POSTER

Fréchet kernels for body wave amplitudes

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We derive a 3-D Fréchet sensitivity kernel relating We derive a 3-D Fréchet sensitivity kernel relating the root-mean-square amplitude of a far-field, broad-band body-wave pulse to laterally heterogeneous seis-mic slowness variations within the earth. Unlike the "banan-doughnut" sensitivity kernel for a cross-correlation traveltime, the amplitude Fréchet kernel for correlation traveltime, the amplitude Fréchet kernel for a turning wave is maximally sensitive, rather than com-pletely insensitive, to the 3-D slowness perturbation along the central source-to-receiver ray. In the asymp-totic limit of an infinite-frequency pulse, our 3-D ampli-tude kernel formulation is consistent with the dominant 1-D integral involving the double cross-path derivative of the slowness perturbation along the unperturbed ge-ometrical ray.

S32C-0642 1330h POSTER

Full Waveform Seismic Inversion With a Time-Variant Sensitivity Equation

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¹Sandia National Laboratories; Geophysical Technology Department, PO Box 5800, Albuquerque, NM 87185-0750 A general approach toward solving the 3D full waveform seismic inverse problem entails iteratively refining a candidate earth model until an acceptable match is obtained between predicted and observed data. On each iteration, we calculate spatially distributed updates to the current model parameters by solving a large system of linear algebraic equations. This system is obtained by determining the sensitivity of each predicted seismic datum (particle displacement) to small perturbations in every model parameter (mass density and elastic moduli) as a function of recording time. These time-variant sensitivity equations are derived by applying the reciprocity principle and the first Born approximation to the velocity-stress equations governing isotropic elastic wave propagation. Construction of the time-variant sensitivity equations is computational generative at the source position and the other activated at the source position and the other activated at the receiver position. Wave propagation through the current estimate of the 3D model is performed with a finite-difference algorithm that solves the elastodynamic velocity-stress system on staggered spatial and temporal grids. For all source-receiver pairs of the acquisition geometry, convolution products are stored at every subsurface gridpoint where parameter updates are desired. The right-hand vector in the linear system consists of displacement residual traces appended end-to-end. We can apply additional linear equations arising from a *priori* constraints' model lease portions of the model space under-constrained). We then use an iterative algebraic solver (also implemented in a parallel computational environment) to seek the minimum-norm, least-squares solution of the attice. eek the minimum-norm, least-squares solution of the entire

entire. We demonstrate this inversion methodology with synthetic seismic data computed for several illustrative earth models, including isolated point diffractors embedded within a smooth background. Point diffractor models allow us to assess the spatial resolving power of the approach, as well as the algorithm's ability to distinguish perturbations in different material properties. For a reflection geometry with sufficient recording aperture, we can recover point perturbations to ρ , λ , or μ with as few as 10 sources recorded into 11 receivers.

F876 2001 Fall Meeting

entropy in exational Laboratories is a multiprogram science and engineering facility operated by Sandia Corporation, a Lockheed Martin company, for the United States Department of Energy under contract DE-AC04-94AL85000.

S32C-0643 1330h POSTER

The Computation of Seismograms in 3D Heterogeneous Media Using Maslov Theory

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Cambridge CB1 2XN, United Kingdom The most efficient methods for modeling seismic waves in heterogeneous media are asymptotic. How-ever, the simplest of these methods (asymptotic ray theory or ART) breaks down near caustics. Caustics are abundant in heterogeneous media. It is therefore necessary to replace ART by a method that is more gen-erally valid. Such methods typically consist of one or two-dimensional integrals over initial slowness or take-off angles. One such method is Maslov asymptotic ray theory (MART). We present a two-dimensional integra-tion method based on Maslov theory. We show how a Maslov amplitude for the integrand can be derived us-ing the method of stationary phase. Then, away from tion method based on Maslov theory. We show how a Maslov amplitude for the integrand can be derived us-ing the method of stationary phase. Then, away from caustics where ART is valid, MART agrees asymptot-ically with ART. The amplitude function has the de-sirable property that it is zero at pseudo-caustics so artifacts are of lower order. The terms needed for the Maslov integrand can all be obtained by standard kinematic and dynamic ray tracing. In order to mini-mize the number of rays shot, triangular ray tubes are formed using the Delaunay algorithm, and an error cri-terion imposed in each tube. Rays are added until the paraxial approximation is accurate for interpolation in all tubes. Thus the integration domain is irregularly sampled and the integration reduces to an integral over irregular triangles. The resultant algorithm is both ef-ficient and accurate. The method is applied to a num-ber of heterogeneous models (both 1D and 3D). It is shown that care must be taken in choosing the integra-tion domain large enough so that all the relevant rays are taken into account.

S32C-0644 1330h POSTER

Seismic Wavefield Extrapolation by Finite–Differencing a One–way **Propagator for Anisotropic Elastic** Media.

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ON K7L 3N6, Canada The narrow-angle approximation to the elastic-anisotropic one-way wave equation derived by Thom-son (1999, GJI, v.137, p.364) lends itself to solution by finite-differences. Several alternative formulations of the finite-difference calculation have been examined (i.e. using the "original" partial differential equation, transformation of the PDE into a system of two cou-pled first-order PDEs and transformation into the fre-quency domain). Finding the optimum finite-difference approach is made complicated by the high dimensional-ity (3D in space and 1D in time) of the PDE, the pres-ence of mixed derivatives and the existence of variable coefficients. In part because of these complications, the coefficients. In part because of these complications, the frequency-domain approach has received most of the development.

development. We have devised two practical extensions to the the-ory. The first involves modification of the "complete" propagator into "separated" wave propagators. This separation allows for the isolation of wavefield modes (i.e. ability to track quasi-compressional or quasi-shear waves individually). The second allows reference

shear waves individually). The second allows reference phase removal, which improves numerical stability with increased step lengths. Preliminary numerical examples have been obtained for (i) the folding (i.e. triplication) of an initially concave wavefront in an isotropic medium and (ii) for quasi-shear waves travelling within a range of direc-tions surrounding a conical point (i.e. around an acous-tic axis). The latter shows the characteristic effects of eigen-polarization rotation. Initial computations have used an equi-spaced Cartesian coordinate grid within a homogeneous model. We have also examined a variable-grid scheme for the lateral/transverse coordi-nates, in order to improve accuracy of the necessary one-sided finite-differences at the boundaries of the domain. domain.

Cartesian coordinates become too limiting for in-Cartesian coordinates become too limiting for in-homogeneous media, where steeply-dipping and turn-ing waves are possible. For such cases an extension to curvilinear coordinates has been applied. These co-ordinates are defined by rays and wavefronts tracked in a possibly-anisotropic reference medium close to the physical medium. Numerical examples using these curvilinear coordinates are in progress, for instance turning waves with a triplication, turning waves with a shadow zone and possibly fractured reservoir and salt structure anisotropy

S32C-0645 1330h POSTER

PML Absorbing Boundary Method: an Application to 3D 4th-order Velocity-Stress Finite-Difference Schemes

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Robust absorbing boundary conditions are central Robust absorbing boundary conditions are central to the utility and advancement of 3D numerical wave propagation methods. In general, it is preferred that an absorbing boundary method be capable of broadband absorption, is easily tuned and is efficient in terms of memory and computational time. Here, we present re-sults on the application of such a method, PML (per-fectly matched layers; Collino and Tsogka, 2001), to a 3D velocity-stress finite-difference scheme. Our elas-tic acheme incomparison surface (Cottaché memor 3D velocity-stress inite-difference scheme. Our elas-tic scheme incorporates a free surface (Gottschämmer and Olsen, 2000) in the internal propagation space as well as in the PML regions. The internal propagation space, which utilizes 4th-order difference operators, is combined with 2nd-order operators in the PML regions. The PML model is formed, for a particular plane re-gion, by partitioning the velocity-stress system based In e FML model is formed, for a particular plane re-gion, by partitioning the velocity-stress system based on perpendicular and parallel spatial derivative separa-tion, with a damping term being added to the perpen-dicular component. For the edges and corners, damp-ing terms are added in all directions for which there are bounding planes. This particular construction the-oretically results in a reflection-free interface between the internal pronaestion snace and the PML absorbing the internal propagation space and the PML absorbing regions

Numerical results for a homogeneous structure. Numerical results for a homogeneous structure, re-alistic source mechanisms and different thickness PML zones are excellent. In general, seismograms produced in conjunction with PML absorbing regions result in no observable reflections compared to the amplitude of the primary phases. Typical amplitude reduction fac-tors (with respect to the maximum trace amplitude) in the presence of Buchish memory and 1000 1/070 and tors (with respect to the maximum trace amplitude) in the presence of Rayleigh waves, are 1/100, 1/250 and 1/500 for PML thicknesses of 5, 10 and 20, respectively. Reduction factors are even greater for body waves only. The PML results are also compared with those of a ba-sic Cerjan et al. (1985) absorbing boundary region of thickness 20, with the PML region of thickness 5 still outperforming the Cerjan et al. method by a factor of 2. Although the PML method requires additional mem-ory for storage of the perpendicular and parallel wave-field variables in the absorbing regions, its computing efficiency and storage requirements, compared to Cer-jan et al., are actually reduced due to the need for only narrow absorbing regions. For example, for our partic-ular model space, a thickness 5 PML scheme required about 80% the memory and 40% the computation time as compared to a thickness 20 Cerjan et al. scheme.

S32C-0646 1330h POSTER

Frequency Domain Seismic Forward Modelling: Staggered Stencils or Star Stencils?

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Modelling seismic wave propagation is essential to quantify site effects and local seismic risk. Numerical results from finite difference (FD) methods are partic-ularly useful as they provide the complete wavefield respon

Frequency domain forward modelling is of special

[•] Frequency domain forward modelling is of special interest for multisource seismic experiments because of their computational efficiency (Pratt, 1990). The system of second-order hyperbolic partial dif-ferential equations is discretized using standard finite difference second-order approximations of derivatives (5-point stencil) on a Cartesian grid. Reduced nu-merical dispersion is obtained by combining deriva-tive discretizations along the Cartesian axis and along the diagonal bisection, which then gives a 9-point star stencil. This stencil incorporates all eight surround-ing points of the center point. In other words, addi-tional averaging coefficients of the FD system are intro-duced into the equation in order to force the coupling of

nearby nodes. Therefore, these coefficients control the numerical dispersion of the FD scheme. Numerical ac-curacy is guaranteed by an optimization technique that determines the averaging coefficients such that the velocity dispersion is minimized.

locity dispersion is minimized. We analyze the strict staggered stencil strategy rather than the ad-hoc star stencil strategy. We con-sider a frequency-space velocity-stress finite difference scheme (1st order hyperbolic system) where derivatives are discretized using the second-order centered differ-ence stencil (-0.5,0,0.5) on a non-staggered grid. Impul-sive punctual source excitation automatically leads to two uncounled staggered grids one is associated with

sive punctual source excitation automatically leads to two uncoupled staggered grids: one is associated with the source node, the other one is left unexcited. This was the reason to cancel out the second grid in order to save memory requirements and lead to the staggered grid geometry. In case of fourth-order FD derivative approxi-mations, the standard centered FD-stencil (1/12,-2/3,0,2/3,-1/12) does not automatically lead to un-coupled staggered grids. The fourth-order extension, namely the 1/12 coefficient, weakly couples the two ex-isting staggered grids, creating unexpected numerical dispersion. Only centered stencils, such as the fourth-order staggered grid stencil (-1/24,0,9/8,0,-9/8,0,1/24), here described on the full non-staggered grid, correctly excites the ad-hoc staggered grid, leaving the second excites the ad-hoc staggered grid, leaving the second grid untouched.

grid untouched. Therefore, we have compared this 9-point staggered stencil and the 9-point star stencil. Numerical disper-sion will be investigated for both the wavelength con-tent and azimuthal variation. We illustrate these re-sults on an example of frequency-domain seismic wave compared in a 20 model.

propagation in 2D media. Pratt, R. G. (1990). Frequency-domain elastic wave modelin by finite-differences: A tool for crosshole seis-mic imaging. Geophysics, 55(5):626-632.

S32C-0647 1330h POSTER

Scattering of P and S Waves by a Spherical Obstacle using the Canonical Solution

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An analysis of the scattering of longitudinal and An analysis of the scattering of longitudinal and transverse elastic waves by a single spherical obstacle using the analytic solution is presented. Our aim is to provide a comprehensive review of this canonical prob-lem and of the resonant scattering theory proposed by Gaunard and Uberall in early eightys. This theory de-scribes the scattering and diffraction of elastic waves by a fluid filled spherical cavity within an elastic solid in terms of a set of summed scattered waves. These partial solutions when analyzed one at time are seen to comsolutions, when analyzed one at a time, are seen to con-sist of two interfering contributions. One is a smooth background corresponding to scattering from an empty cavity, and the other is a superimposed set of resonant spectral spikes (lines with narrow width) of the filler fluid. In this work we discuss how these modal reso-nances and their band widths, which have been only calculated for incident P waves and very specific lo-cations, can be studied also for incident S waves and arbitrary observation points. In fact, we propose that the usefulness of this theory to establish an identifica-tion pattern for the fluid filler is not restricted only to the P waves. The calculations presented here are carried out an-alytically, within the framework of elastic theory withsolutions, when analyzed one at a time, are seen to con-

The calculations presented here are carried out an-alytically, within the framework of elastic theory with-out any additional approximation. A catalog of the appropriate analytical expressions is provided in terms of both the spherical Bessels and Legendres functions. We believe our expressions are free of typographical errors (that have plagued the literature of the field). We study the cases in which the sphere is either (1) a cavity, (2) an elastic inclusion or (3) a fluid inclu-sion. Spectral amplitudes versus normalized frequency and synthetic seismograms for the three components of movement are depicted. 2D and 3D scattering patterns and real time snapshots are given to analyze the main propagation features.

S32C-0648 1330h POSTER

A Wavelet-Based Method for Simulation of Seismic Wave Propagation

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Seismic wave propagation (e.g., both P-SV and SH in 2-D) can be modeled using wavelets. The gov-erning elastic wave equations are transformed to a first-order differential equation system in time with a displacement-velocity formulation. Spatial deriva-tives are represented with a wavelet expansion using a semigroup approach. The evolution equations in time are derived from a Taylor expansion in terms of wavelet operators. The wavelet representation allows bigh accuracy for the spatial derivatives. Absorbing boundary conditions are implemented by including at-tenuation terms in the formulation of the equations. The traction-free condition at a free surface can be tenuation terms in the formulation of the equations. The traction-free condition at a free surface can be introduced with an equivalent force system. Irregu-lar boundaries can be handled through a remapping of the coordinate system. The method is based on a displacement-velocity scheme which reduces mem-ory requirements by about 30% compared to the use of velocity-stress. The new approach gives excellent agreement with analytic results for simple models in-cluding the Rayleigh waves at a free surface. A major strength of the wavelet approach is that the formula-tion can be employed for highly heterogeneous media and so can be used for complex situations.

S32C-0649 1330h POSTER

Fast Phase Space Computation of Multiple Arrivals

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We present a fast, general technique for comput We present a fast, general technique for comput-ing multiple-arrival traveltimes in seismological prob-lems.Using the Liouville formulation of the character-istic equations as a starting point, we derive a set of "Bscape Equations" which are static, time-independent Eulerian partial differential equations with prescribed boundary conditions which represent all arrivals to the surface from all possible sources in the subsurface. The solution may be parameterized as a family of hypersur-faces; which we numerically produce through a one-pass formulation, building on ideas from semi-Lagrangian methods and Fast Marching methods. Unlike a ray-tracing approach, which starts with a given set of sources and recomputes the entire solution each time these sources are changed, in this formulation the same result is achieved in postprocessing once the essential solution has been obtained. We demonstrate the algo-rithm by showing multiple arrivals in a variety of vesolution has been obtained. We demonstrate the algo-rithm by showing multiple arrivals in a variety of ve-locity fields, corresponding to complex geological situ-ations. In addition, we show how the same techniques can be used to compute the wave amplitudes and ex-tract the most energetic arrival.

S32C-0650 1330h POSTER

Scattering of elastic waves by an arbitrary shaped 3-D planar crack using the Indirect Boundary Element Method

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The scattering of elastic waves by various types of The scattering of ensite waves by various (types of cracks is an important engineering problem. From a physical point of view the question that arises is up to what degree will a local perturbation in a medium mod-ifies the scattered wave field. For instance, in the seis-mic monitoring to enhance oil recovery (due to exten-sive presence of cracks and cavities) a crucial problem is to determine zones where there are physical property changes. Modelling such highly heterogeneous media is is to determine zones where there are physical property changes. Modelling such highly heterogeneous media is critical to increased production from oil and gas. In order to study scattering effects caused by arbitrary-shaped cracks a simplified indirect boundary element method (BEM) is used to compute the seismic response of a 3-D crack under incident elastic P and S waves. The method is based on the integral representation for scat-tered elastic waves using single layer boundary sources. This approach is called indirect BEM in the literature as the sources strengths should be obtained as an in-termediate step. Scattered waves are constructed at the boundaries from which they radiate. Therefore, this method can be regarded as a numerical realiza-tion of Huygens' principle. Boundary conditions lead

a system of integral for boundary sources. A sim-fied discretization scheme is used. It is based on plified discretization scheme is used. It is based on the approximate rectification of the surfaces involved the approximate rectification of the surfaces involved using circles for the numerical and analytical integra-tion of the exact Green's function for the unbounded elastic space. Radiation patterns for penny-shaped and croissant-shaped cracks are explored. The scattering effects of the elastic waves in a homogeneous isotropic infinite elastic medium with a 3-D crack are displayed in both frequency and time domains in both frequency and time domains

S32C-0651 1330h POSTER

Modeling and Processing of Continuous 3D Elastic Wavefield Data

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Continuous seismic wavefields are excited by earth-quake clustering, induced seismicity in reservoirs, and mining. In hydrocarbon reservoirs, for example, pore pressure changes and fluid flow (mass transfer) will cause incremental deviatoric stresses sufficient to trigmining. In hydrocarbon reservoirs, for example, pore pressure changes and fluid flow (mass transfer) will cause incremental deviatoric stresses sufficient to trig-ger and sustain seismic activity. Here we address three aspects of seismic wavefields in three-dimensional het-erogeneous media triggered by distributed sources in space and time: forward modeling, multichannel data processing, and source location imaging. A power law distribution of seismic sources (such as the Gutenberg-Richter law) is used for the modeling of viscoelas-tic/elastic wave propagation through a realistic earth model. 3D modeling provides new insight in the in-teraction of multi-source wavefields and the role of scale-dependend elastic model parameters on transmit-ted and reflected/back-scattered wavefields. There ex-tists a strong correlation between the spatial proper-ties of the compressional, shear wave and density per-turbations and the lateral correlation length of the resulting reflected or transmitted seismic wavefields. Modeling is based on the implementation of 3D elas-tic/viscoelastic FD codes on massive parallel and/or distributed computing resources using MPI (message passing interface). For parallelization, large grid 3D earth models are decomposed into subvolume process-ing elements wherehey each processing element is updat-ing the wavefield within its portion of the grid. Pro-cessing of continuous seismic wavefields excited by mul-tiple distributed sources is based on a combination of crosscorrelated or slowness-transformed array data and Kirchhoff or reverse time migration for source location or source volume imaging. The appearance of slowness the possibility of combining them into a single process. In order to place further constraints on the migration, the directivity properties of 3-component receiver arthe possibility of combining them into a single process. In order to place further constraints on the migration, the directivity properties of 3-component receiver ar-rays can be included in the processing sequence. Con-tinuous seismic array data from both borehole and sur-face seismic acquisition geometries are suitable for the proposed detection and mapping sequence for acoustic emission data in space and time.

S32C-0652 1330h POSTER

Efficient 3D Hybrid Ray-FD Modeling for Elastic Media with Locally Complex Structures

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A new hybrid ray-FD method combines the ray and A new hybrid ray-FD method combines the ray and the 2nd order finite-difference (FD) approaches. It was designed for computations in large (compared to the wavelength) 3D elastic models containing a complex lo-cal (inner) structure embedded in a considerably sim-pler medium (outer structure). The hybrid method is based on two successive steps.

The hybrid method is based on two successive steps. In the first step, the wavefield propagating in the outer structure is calculated by the ray method. It is inci-dent at the points along a two-fold formal boundary (excitation box, EB) surrounding the inner structure. This provides the input for the second step consisting in calculating the wavefield by the FD method. The FD computational domain contains the EB and its close vicinity. The EB remains fully permeable for all waves propagating within the FD domain. Asymptotic high frequency solution makes the ap-proach very efficient despite of the two-point ray trac-ing that is required to connect the source point with the excitation gridpoints. 3D rays are necessary due

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to arbitrary source-EB configuration, even in ca outer structure is less dimensional (2D, 1D, ho neous). However, it is still much faster than the homoge whole neous). However, it is still much faster than the whole FD modeling (retaining the advantages of the FD so-lution) provided the outer structure does not contain too many layers. Then this approach benefits from the efficiency of the ray method in the outer structure while exploiting the wavefield completeness of the FD method method

The hybrid method is applied for models in which The hybrid method is applied for models in which the locally complex structure is adjacent to the earth surface and includes topography. The wavefield is due to a double-couple source buried in the outer struc-ture. The outer structure is 1D or 2D containing verti-cal as well as lateral gradients of medium parameters. The former case allows the results to be compared with DWN-FD hybrid approach replacing the ray method in the first step by discrete wavenumber (DWN) method.

S32C-0653 1330h POSTER

Rapid Generation of Synthetic Seismograms by Reduced Path Integration

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Recently, a path integral solution, or sum over all paths, for acoustic wave propagation has been devel-oped. However, the difficulty with the application of the acoustic path integral is that the contribution of each path is highly oscillatory. In principle, construc-tive and destructive interference between nearby paths will smooth out the end result, but such interference is nearly impossible to achieve numerically. With a reawill smooth out the end result, but such interference is nearly impossible to achieve numerically. With a rea-sonable approximation, we can account for the contri-bution of all but the smoothest paths, greatly reducing the dimensionality of the path integral and smoothing the contribution of each path to yield a formula of con-siderable utility. Several comparisons between the re-duced path integral method and slower, established nu-merical methods for nontrivial 3D media will be made.

S32C-0654 1330h POSTER

Time-Domain Sensitivities for Elastic Wavefield Data

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ogy Department , PO Box 5800, Albuquerque, NM 87185-0750, United States Exact mathematical expressions for the sensitivity of elastic wavefield data, with respect to small perturbations in mass density and Lame parameters, are derived by applying the reciprocity principle to solutions of the velocity-stress differential equations of various types of sources (forces, moments, surface traction, strain, rotation, pressure) used in seismic exploration, and apply to arbitrary data acquisition configurations in three spatial dimensions. Sensitivities with respect to variations in other elastic model parameters of seismological interest (wavespeeds, impedances, moduli) are readily obtained via linear combinations of the sensitivities due to perturbations in ρ , λ , and μ . Bandlimited sensitivity coefficients are numerically calculated with a time-domain finite-difference algorithm that solves the velocity-stress system on staggered spatial and temporal grids. For a given source position and the other is activated at the source position in the other is activated at the receiver positions in mass density. Convolution for herturbations in mass density. Convolution for herturbated for a simple situation consisting of a single source-receiver pair located within a homogeneous and isotropic elastic wholespace. Timeslice lots of λ sensitivity indicate that significant amplitudes are concentrated are that significant amplitudes are concentrated are concentrated are concentrated are concentrated are the source for a simple situation consisting of a single source-receiver pair situated within a homogeneous and source-receiver pair situated within a homogeneous and the other singlificant amplitudes are concentrated arond the ellipsoidal locus of fixed-time P-to-P-scattering from source to receiver. Plots of ρ and μ

tivity indicate that significant amplitudes are concen-trated around the ellipsoidal locus of fixed-time P-to-P scattering from source to receiver. Plots of ρ and μ sensitivity are much more complex, containing multi-ple branches corresponding to P-P, P-S, S-P, and S-S scattering. Parameter sensitivities are used for solv-ing the full waveform elastic inverse problem, and may provide useful information for design of seismic data accusibility experiments.

acquisition experiments. Sandia National Laboratories is a multiprogram science and engineering facility operated by Sandia Corporation, a Lockheed-Martin company, for the US Department of Energy under contract DE-AC04-94AL85000

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S32C-0655 1330h POSTER

Array analysis of seismic signals considering an array beampattern

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gash 1-1-1, Tsukuba 305-8567, Japan Seismic array data have been widely used in re-searches such as the discrimination of nuclear explo-sions, the analysis of seismic scattering, measurements of surface wave dispersion, and monitoring of the seis-mic activity in volcanic areas. In this study, we present a simple and high-resolution array processing method whose estimators are not pseudo but true ones. We ap-ply the method to estimations of high-frequency rup-ture processes by converting temporal variations in slowness vectors and their associated amplitude into power distributions and rupture times on the fault plane. plane

power distributions and rupture times on the fault plane. It has been shown that the minimum variance dis-tortionless (HR) method and the multiple signal classi-fication (MUSIC) method produce higher resolution for the location of the identified waves than the standard Fourier method (CV method). However, the estimators by the HR and MUSIC methods are pseudo ones. In order to obtain true spectral estimators with high resolutions, we propose a frequency-wavenumber method considering an array beampatterm. The ob-served power spectrum obtained by the CV method is a convolution of the array beampatterm reduces the resolution of the spectral estimators, we deconvolve the observed power spectrum with the array beampat-tern in the wavenumber domain. The solution to this problem is determined using non-negative least squares because the power has a positive quantity. because the power has a positive quantity. To illustrate the utility of the present method in re-

To illustrate the utility of the present method in re-solving two closely separated signals, numerical tests are performed with synthetic waves. The present method successfully resolved two separate peaks at al-most the correct slowness vectors. The resolution was superior to CV and HR methods and similar to MU-SIC method. We then investigate the applicability of the present array processing method to estimations of high-frequency rupture processes. Using synthetic S body-wave seismograms from extended earthquake sources, we show that it is possible to image high-frequency source locations and their associated rupture times with high resolutions.

S32C-0656 1330h POSTER

Estimation of the Wavelet Correlation **Dimension of Surfaces in Acoustic Back-Scattering Experiments**

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15 53 144 15 Potsdam Germany ²Geosciences Rennes, Campus de Beaulieu 35042 Rennes France We show how to extract from the backscattering data in the 1 dimensional wave equation the wavelet correlation dimension of the scatterer. The wavelet correlation dimension is a generalization of the stan-dard fractal correlation dimension defined for proba-bility measures. This technique is applied to the esti-mation of the rugosity of a natural granite surface in an acoustic small scale experiment. We present a wavelet based procedure for deconvolution from the measure-ment device. A stacking method based on the small amlitude approximation allows the estimation of the orientation of the local incidence plane.

S32C-0657 1330h POSTER

Robust Waveform Inversion with Adaptive Regularization

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Derivation of detailed maps of elastic properties in The seismic frequency band and beyond is a highly chal-lenging task. Global optimization methods have been highly successful in that they are not dependent on the choice of starting solution, they explore the model space extensively and reflections from all angles in-cluding post-critical arrivals can be included without difficulty. However for large models, they are compu-tationally intensive and they are more prone to non-uniqueness. Regularization in global optimization is trivial, in theory but difficult in practice since it slows down the algorithm. We have developed local optimiza-tion methods with adaptive regularization that can be used efficiently in conjunction with global optimiza-tion for analysis of large volume of seismic data. In particular, our conjugate gradient-adaptive regulariza-tion scheme has been implemented on three processes that are vital to seismic data analysis, namely, wavelet tion scheme has been implemented on three processes that are vital to seismic data analysis, namely, wavelet estimation, impedance inversion from post-stack data and pre-stack inversion for estimation of Vp, Vs and density. Use of a new method of computing differen-tial seismograms combined with sparse gradient ma-trix makes our algorithm computationally very effi-cient. We have applied these techniques successfully in the analysis of field data from the Gulf of Thailand and the Oregon coast. and the Oregon coast.

URL: http://www.ig.utexas.edu

S32C-0658 1330h POSTER

Imaging of Crustal Layers by Teleseismic Ghosts

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West Lafayette, IN 47006, United States We propose imaging of crustal reflector distribu-tions by migrating ghost reflections extant in tele-seismic records. Ghost reflections emanate from di-rect waves that reflect off the free-surface, and prop-agate downward to reflect from crustal layer inter-faces. These ghost reflections can be imaged by the new method of cross-correlogram migration. The recording requirements for this passive seismic method are sim-ilar to those for exploration seismology: an unaliased recording array which might be attainable with the pro-posed US Array. Unlike controlled source seismology, the recorded traces are crosscorrelated with one an-other and the correlated traces are migrated using a special imaging condition (Schuster, 2001, EAGE Ams-terdam annual meeting). The benefit is that the source location or the wavelet time history do not need to be known; the drawhack is that correlation produces spu-rious events that can give rise to false reflector images. rious events that can give rise to false reflector images. With special processing and records from different tele-seisms, these spurious events can sometimes be sup-pressed. It can also be shown that crosscorrelogram migration with special imaging conditions is a gener-alization of receiver-function imaging of PS converted waves. We will show examples of imaging crustal reflec-tors by migrating ghost reflections in synthetic teleseis-mic data for a Utah crustal model.

S32C-0659 1330h POSTER

Velocity Structure Determination Through Seismic Waveform Modeling and Time Deviations

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Louis, MO 63103 Through the use of seismic waveforms recorded by TriNet, a dataset of earthquake focal mechanisms and deviations (time shifts) relative to a standard model fa-cilitates the investigation of the crust and uppermost mantle of southern California. The CAP method of focal mechanism determination, in use by TriNet on a routine basis, provides time shifts for surface waves and Pnl arrivals independently relative to the reference model. These shifts serve as initial data for calibration of local and regional seismic paths. Time shifts from the CAP method are derived by splitting the Pnl sec-tion of the waveform, the first arriving Pn to just before the arrival of the S wave, from the much slower surface waves then cross-correlating the data with synthetic waves interact with the entire crust, but the upper rust causes the greatest effect. Whereas, Pnl arrivals sample the deeper crust, upper mantle, and source re-gion. This natural division separates the upper from

lower crust for regional calibration and structural mod-

lower crust for regional calibration and structural mod-eling and allows 3-D velocity maps to be created using the resulting time shifts. Further examination of Pnl and other arrivals which interact with the Moho illuminate the complex nature of this boundary. Initial attempts at using the first 10 seconds of the Pnl section to determine upper most mantle structure have proven insightful. Two large earthquakes north of southern California in Nevada and Mammoth Lakes, CA allow the creation of record sec-tions from 200 to 600 km. As the paths swing from east to west across southern California, simple 1-D models turn into complex structure, dramatically changing the to west across southern California, simple I-D models turn into complex structure, dramatically changing the waveform character. Using finite difference models to explain the structure, we determine that a low velocity zone is present at the base of the crust and extends to 100 km in depth. Velocity variations of 5 percent of the mantle in combination with steeply sloping edges produces complex waveform variations. Characteristics of this complex propagation appear from the southern Sierra Nevada Mountains, in the west, to Death Valley in the east. The structure does not cross the Garlock fault to the south, but we are unsure of the structures northern extent.

S32C-0660 1330h POSTER

Fractional Brownian Motion in Seismic Noise

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Via Fosso del Cavaliere 100, Roma 00133, Italy Here, we present a preliminary study of the statisti-cal features of the seismic noise in the frequency range from 1 Hz to 40 Hz. In detail, we have investigated the 3-d average squared soil displacement r^2 and the distribution function of the displacement fluctuations in different geological sites. The anomalous scaling of the squared displacement $r^2 \simeq t^{\alpha}$ with $1.5 \leq \alpha \leq 2$, and the Gaussian shape of the fluctuation distribution function sugrest that seismic noise, when studied in and the Gaussian shape of the fluctuation distribution function suggest that seismic noise, when studied in the limit of ground shaking, is consistent with a persistent fractional browian motion (FBM) characterized by a Hurst exponent $H > \frac{1}{2}$. A brief discussion of our results in connection with seismic radiation transport in heterogeneous geological media is also given.

S32D MC: 306 Wednesday 1330h Strong Ground Motion Prediction for Scenario Earthquakes II (joint with PA)

Presiding: R Graves, URS

Corporation; D Wald, U.S. Geological Survey

\$32D-01 1330h INVITED

Practical Applications for Earthquake Scenarios Using ShakeMap

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Technology, Pasadena, ČA 91125, United States In planning and coordinating emergency re-sponse, utilities, local government, and other or-ganizations are best served by conducting train-ing exercises based on realistic earthquake situa-tionsones that they are most likely to face. Sce-nario earthquakes can fill this role; they can be generated for any geologically plausible earthquake or for actual historic earthquakes. ShakeMap Web pages now display selected earthquake scenar-ios (www.trinet.org/shake/archive/scenario/html) and more events will be added as they are requested and produced. We will discuss the methodology and pro-vide practical examples where these scenarios are used directly for risk reduction. directly for risk reduction. Given a selected event, we have developed tools to

make it relatively easy to generate a ShakeMap earth-quake scenario using the following steps: 1) Assume a particular fault or fault segment will (or did) rupture over a certain length, 2) Determine the magnitude of